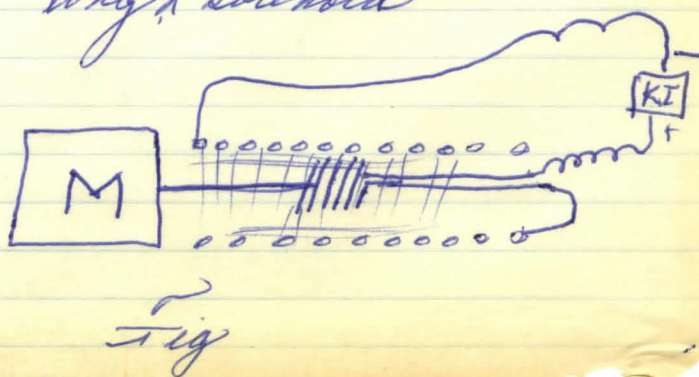
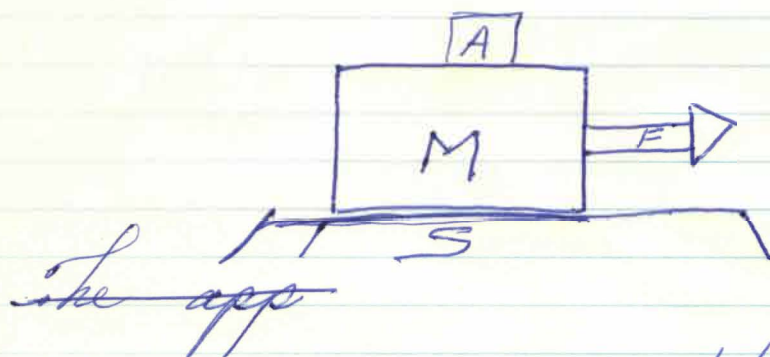


$$M = \frac{F}{A}$$

~~One of the~~ An apparently simple method of mass determination would require only a constant force & measurement of the acceleration produced. A variety of forces are available but ~~not~~ ^{all} are ^{only relatively} constant. ~~Some of the~~ ^{available} constant force generators which could be used are gas jets, constant force springs, and electro-magnetic and constant pressure gas cylinders pistons. It will be assumed that the final velocity obtained is low and that acceleration is small. It is difficult to put performance values on the various methods but ^{an} electro-magnetic scheme would probably be ~~useful~~ the most accurate ^{force} arrangement, especially for small forces. ~~Such~~ Fig - — shows one possible arrangement in which a long solenoid develops a constant magnetic field. In series [&] this long solenoid



A schematic of this arrangement is shown in Fig I.



M is a mass ~~supported & constrained~~ ^{along} ~~on~~ a ^{single} ~~given~~ axis by the support S. This device ^{constraint} ~~must~~ should be frictionless and at or at least ^{must} have a constant coefficient of friction. A constant force F is applied and will be balanced by a number of other forces including the desired inertial force, wind drag, ~~and~~ inertial force from "trapped" air, ^{resistive forces} ~~and resistance~~ from any mechanical drag of the ~~restraining~~ arrangement, and if the body is non rigid complex forces from "slosh" of the movable portions and ^{the effects} ~~of~~ any internal force generators ~~are~~ present such as the heart in humans. ~~High~~

Acceleration may be measured directly from

an accelerometer mounted on the mass. ~~or~~
 A ~~more~~ ^{more} practically alternative to the accelerometer is
~~some~~ ~~an~~ an arrangement which measures the
 time required to traverse a fixed distance from
 which average acceleration may be determined from
 $S = \frac{1}{2} g t^2$. The latter method has the advantage
 of using time, ~~our most accurate~~ the quantity which can
 generally be determined to greatest ease and accuracy,
 and of removing ~~an~~ a heavy & expensive bit
 of instrumentation from the "pan" carrying the mass.

$$\begin{aligned} \frac{F}{M} &= MA \\ \text{Dist} &= \frac{1}{2} \text{acceleration} (\text{time})^2 \\ &= \frac{\text{Force} \cdot \text{time}^2}{2 M} \end{aligned} \left\{ \begin{aligned} T &= \sqrt{\frac{2 \text{ mass dist}}{\text{Force}}} \end{aligned} \right.$$

From the above equations the rates of change of
 mass i.e. errors may be determined w respect to
 the other variable rates of change (error) in other
 quantities - $\text{Mass} = K \cdot \frac{\text{Force} \cdot \text{Time}^2}{\text{Dist}}^{-1}$

Holding const: force & time $\frac{dM}{M} = \frac{d \text{Dist}}{D}$
 $\frac{dM}{M} = K \frac{dD}{D}$

dist. + force

$$dM = K 2T dt$$

&

$$\frac{dM}{M} = K \frac{2T dT}{T^2}$$

Time + dist.-

$$dM = K dF$$

&

$$\frac{dM}{M} = K \frac{dF}{F}$$

From these considerations certain elementary conclusions may be drawn. If the error in knowledge of the distance is reasonably constant then the distance should be as large as possible. ~~The~~ Error in distance, which may arise from temperature dependent expansion and the like, must be carefully guarded against.

Time errors will be multiplied by two and again all other things being equal the time period should be as long as possible which is consistent with a long distance.