

Mass-General

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FEDERAL SUPPLY SERVICE

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The measurement of mass -

Although mass is one of the fundamental physical quantities its ^{physical} value is ^{derived} ~~is made~~ ^{from measurements} ~~in terms~~ ^{usually} of other quantities that relate to motion.

In ^{relation to} ~~terms~~ of force the general equation for motion of a mass is

$$F^2 = (MA)^2 + \frac{M^2 V^2}{4}$$

F = Force
M = Mass
A = Acceleration
V = Velocity

~~The almost universal measurement of mass is dependent upon the first term of the equation where the~~

The first term of the equation relates to linear motion while the second ~~term~~ deals with radial motion.

The almost universal measurement of mass is

dependent on a relatively constant acceleration or field (gravity) such as on earth is dependent is described by the first term of the equation

$F = M A$ - The force developed by the mass (or more commonly the ratio of forces) in the field of acceleration of $M/sec/sec.$ is measured.

In the ^{negation} ~~absence~~ of such a field, acceleration or some other quan. must be applied and the resultant effects measured. The ^{quantities of motion} ~~quantities~~ effects that must be applied and those that may be ~~measured~~ ^{can} be determined ^{from} ~~by~~ ~~an~~ arrangements of the general equation.

1.1. 1st Term: $F = M A$

	Applied or Known		Desired		Meas.
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1.1.1	A	x	M	=	Force
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1.1.2	Force	÷	M	=	Acceleration
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1.2 2nd Term: $F = \frac{1}{2} M V^2$

1.2.1	Velocity		M	•	Force
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1.2.2	Force		M		Velocity
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2 - physical limits tolerated by the human body

Although not immediately apparent, mass by means of this equation and known restoring forces provided by an elastic medium, the mass may be determined as a function of ~~so~~ time of oscillation. These equations will be described later.

The measurement of mass under weightless conditions will become as routine and accurate as it currently is on the earth's surface - The difference at the moment is several thousands of years of experience ~~in a free force field~~ in a ubiquitous gravity.

The measurement of ^{the mass of} man in current space conditions imposes a number of restrictions including ~~non~~

1. non-rigidity of the human body

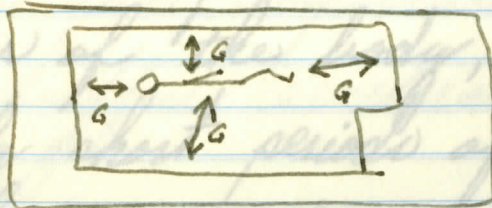
~~2~~ 2 - physical limits tolerated by the human body

3. Minimum instrumentation including space, power, time, operational simplicity
4. Relatively high accuracy (approx. 0.1% or 1 part in 1000)

A considerable amount of theoretical work and a ~~more~~ much smaller amount of experimental work has been done on the problem which will be reviewed as a function of the various possible approaches.

$$\text{Force} = \text{Mass} \times \text{Acceleration}$$

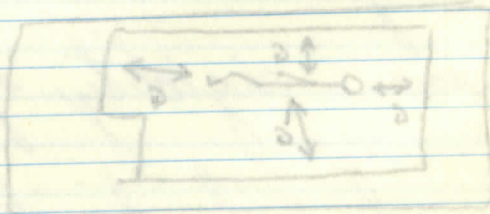
The gravitational force developed by ^{masses} ~~objects~~ traveling in orbit $\bar{c}$ man are much too small, irregular and variable to be considered.



$$G = \frac{m_1 m_2}{D^2}$$

* Even if rigorous control of the external body is maintained plus cessation of respiration, the heart & to and viscera are in more or less continuous motion although the heart displacement of mass is cyclic.

$$C = \frac{m \cdot m}{\rho^2}$$



$$A = \frac{F}{M}$$

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A wide variety of schemes, some quite practical are possible through application of known or measured forces and in a linear axis $\bar{c}$ measurement of acceleration or its ^{integrals, velocity} derivatives, distance, & time.

One of the ^{more} critical, if not most critical aspects of the measurement will be in the proper application and of forces to the body in a desired reference system and deserves special comment.

The flexibility of the body causes a number of problems. The body seldom maintains a fixed configuration for an appreciable length of time. Even if one makes vigorous attempts to maintain a fixed relationship of the various members of the body, this ~~can~~ can be maintained for only short periods of time. The evidence of this may be seen on the parade ground.*

one aspect
 The practical importance of this is that the measurement should be of short duration, calculation ~~and~~ the consequences of the flexibility of the body are the requirements that acceleration be kept below a value which causes shifts in their ^{spatial} relationship. To each also any measurement which depends upon establishment or maintenance of a fixed center of mass for more than a short period will be done only with great difficulty.

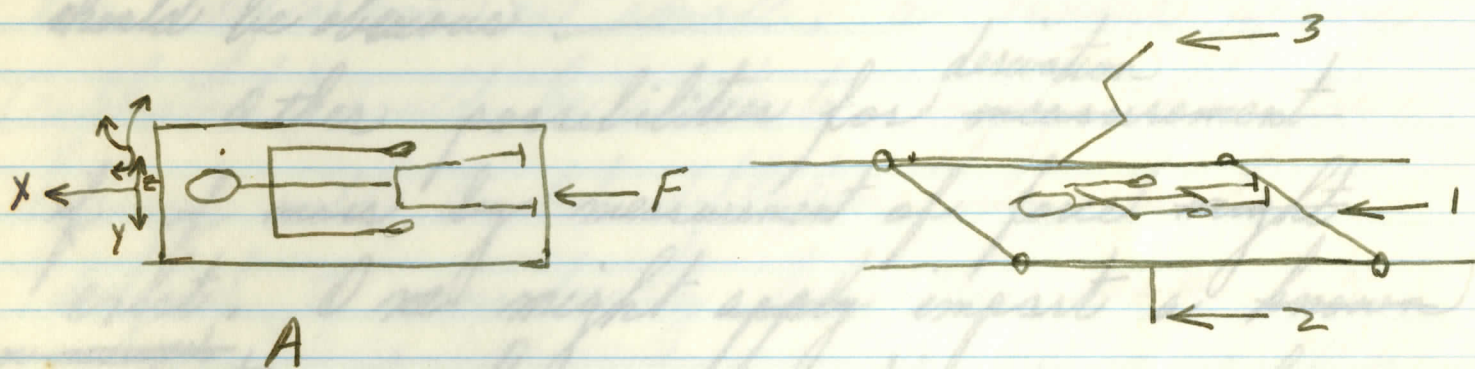
The values of acceleration required to produce shifts of various segments of the body are not readily available.

reports on this in terms of frequency of sinusoidal oscillation but unfortunately does not give amplitudes of the test values so that meaningful accelerations cannot be determined.

It would appear then that the

especially in the vertical plane shown here -

A corollary of rigid fixation is application of forces and measurement in such a manner that only the desired directions are achieved - Examples are shown below -



In A the table and subj. are ^Bweightless and free to move in 6 axes, three translational or linear (XYZ) and 3 rotational.

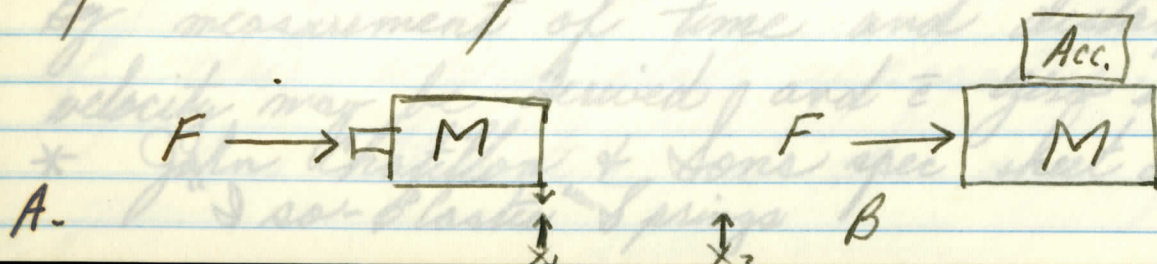
If the force applied at F is not ^{at} along the center of mass in the YZ plane movement can (and will) occur in all six of these planes. This situation is obviously intolerable for simple measurement -

In B the table and man are constrained by four frictionless bearings to move only in the X axis. The force (or X component of force), ^{and measurements} may now be applied at any point in the Y, Z plane that is rigidly attached to the ~~table~~ table. The advantages should be obvious.

Other possibilities for ^{derivation} measurement of mass by measurement of force might exist. One might apply impart a ~~known~~ ^{or measured} velocity to the mass and measure the force to provide required to produce known or measured decelerations.

$$A = \frac{F}{M}$$

A wide variety of practical schemes, ^{some} many of which might be practical are possible here.



~~Q~~ In A the mass is accelerated past two points of known distance x_1 & x_2 by a known or measured force F (~~it~~ preferably this force would be constant). ~~Good~~ Production of this standard force would be difficult. Assuming the deflection is small, a linear spring (calibrated) could be used to supply this force. Springs with limited deflection may be designed $\pm$ considerably less than $\pm 0.1\%$ deviation of force as a function of distance with temperature coefficients of $< 10^{-5}\% / ^\circ F$ and hysteresis ^{error} of 0.05% of deflection*.

The measurement of both distance and time may be may with simple instrumentation (Capacitance or optical pickups $\pm$ errors of say ~~1-2~~ $1-2 \times 10^{-4}$ " & counters $\pm$ accuracy of $\pm 1 \times 10^{-6}$ sec)

By measurement of time and distance velocity may be derived and $\pm$ zero initial velocity
* John Chatillon & Sons spec sheet on "Iso-Elastic" Springs

$$1. \quad \text{Distance} = \frac{1}{2} a t^2 + A = \frac{2 \text{ dist}}{T^2}$$

and from this acceleration & mass, a possibility more accurate arrangement to avoid starting errors, ^{effects of} a shift in viscera etc would have measure distance velocity over two spr distances. The first derived velocity would then be used ^{with} the 2^o velocity to determine acceleration from $D = V_1 + \frac{1}{2} a t^2$

$$+ 2 \frac{(D - V_1)}{t^2} = a$$

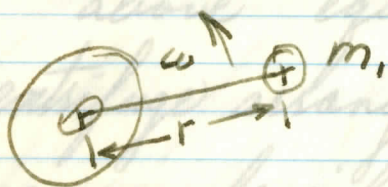
A simpler ~~and~~ variation of this ^{scheme} will using an oscillating spring-mass system will be described later. Other ~~or~~ sources of ^{known} force include long solenoids & possibly small ^{compressed} gas jets. Lockheed A/C investigated this scheme using a spring wound capstan and a wooden trolley. Accuracy was only a few percent which is not surprising ~~using~~ & considering the crudity of their experimental apparatus.

An alternative is the use of

a relatively constant force which is accurately measured by means of a strain gage or other arrangement. Although NBS* states that force meas. of $< .1\%$ may be "easily" achieved, a commercial mfg. would not consider a guarantee of $< .5\%$.

A more direct approach might be the arrangement in B in which the acceleration is meas. directly $\bar{c}$ an accelerometer. Here again accuracy of the accelerometer is a problem.

One common source of a known ^{sinusoidal} force is the rotating bob out. If r, ω & m , the



radius r & angular rate ω of rotation of the mass m , is known

a standard force is provided. Although this could be used directly an alternative is to provide rigidly attached a $\approx 2''$ mass free to oscillate along the plane of

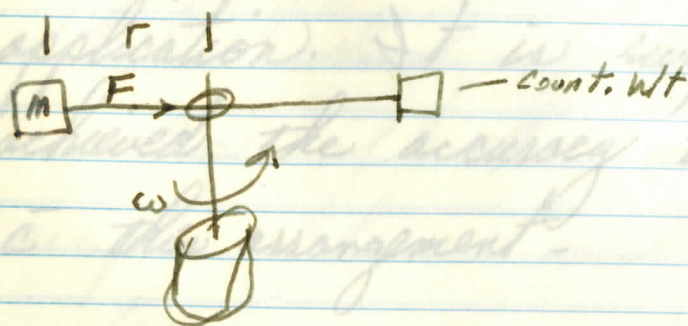
* personal communication $\bar{c}$ metrology dept. NBS
 $\bar{c}$ Satham Instruments

rotation. The amplitude of rotation sinusoidal oscillation of the 2nd mass m_2 will then be an inverse ratio of the $m_1:m_2$ ratio and ~~an~~ radius of rotation r . - Accessory equipment and accuracy problems of the amplitude transducer reduce the attractiveness of this scheme.

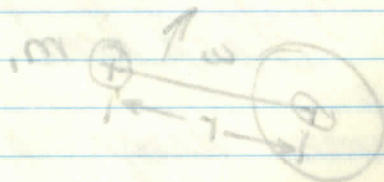
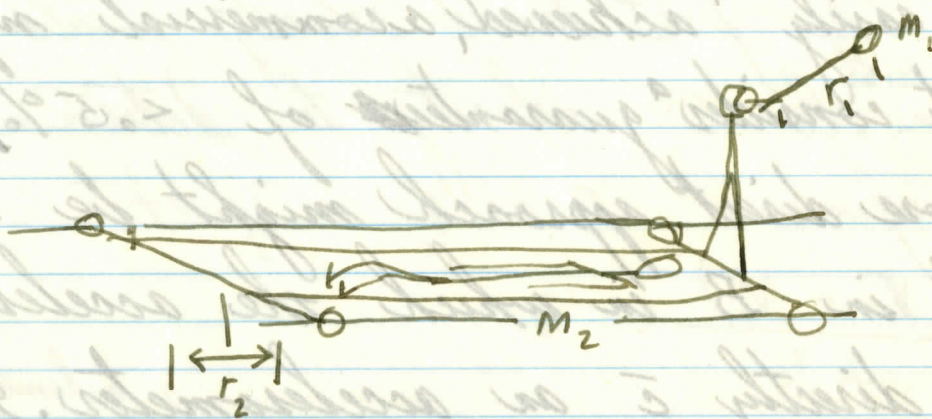
In addition ^{angular} rotational motion may ~~us~~ be used in these applications rather than linear but in general angular rate, distance & force meas. are more difficult than linear.

$$F = \frac{1}{2} m v^2$$

The above equation leads immediately to a centrifuge arrangement. Although this seems plausible and may be made work with small fixed weights



Even here the the problems of knowing center of mass and accurately



measuring mass ~~ex~~ still apply. The problem of ~~force~~ ^{rotating} measurement is compounded by ~~the~~ by its being in rotation and angular rate must also be known to a high degree of ^{greater than} the desired degree of accuracy ~~since~~ since this term is squared.

The use of a centrifuge as a mass measurement of man can be of only academic interest unless one has a centrifuge to sell and has allowed cupidity to overcome realism. The man would have to be measured at two radii of rotation to attempt to overcome the problem of lack of knowledge of center of mass. The size and complexity of instrument and instrumentation are enough to veto this application. It is surprising that Douglas achieved the accuracy they did (several %) ~~in~~ this arrangement.

~~At +~~ If one considers other equations for deriving mass in terms of other quantities and gives to free rein to imagination a variety of scheme may be devised that are in the centrifuge class.

For example for mass has energy associated $\bar{c}$ it :

$$E = \frac{1}{2} m V^2$$

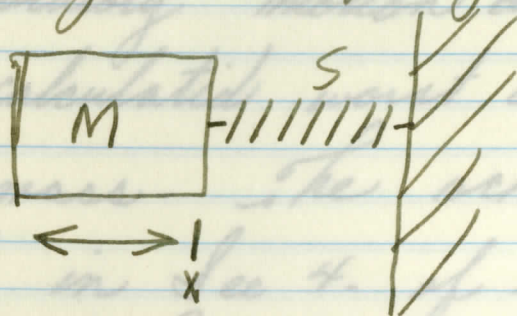
After ~~By~~ giving the mass^m a known velocity v (or meas. it) ~~the mass m could be~~ it could be decelerated to zero velocity in by a thermally isolated resistive media and the resulting temperature change measured.

A mass m ~~cont~~ $\bar{c}$ velocity v could be allowed to collide $\bar{c}$ a 2^o elastic mass, say through a spring, and the resultant velocity of the 2^o mass measured to ~~determine velocity of v~~ derive mass.

One of the more attractive $\vec{v}$ and simple schemes involve determination of frequency or period of the mass

in an oscillating spring/mass system.

If the mass m , is attached to a system spring which provides a



restoring force as a function of distance spring length s and

the mass is displaced

from zero and allowed to move freely it will perform a damped sinusoidal oscillation.

~~Damp~~ The damping, or decrease in oscillation $\propto$ time is a function of the amount of spring dissipation $\propto$ air, resistance. If the resistance is great enough an exponential return to zero will occur. Frequency of the oscillation ~~is~~ is given by

$$F = \frac{1}{2\pi \sqrt{M \left(K - \frac{R^2}{4M} \right)}}$$

If as is usually the case

R is small the R^2 term

may be neglected $\therefore$

$M = \text{Mass}$

$K = \text{spring constant}$

$T = \text{period of time}$

$$F = \frac{1}{2\pi \sqrt{M K}}$$

$$\& T = 2\pi \sqrt{\frac{M}{K}}$$

$$\alpha \approx \tau \cdot \sqrt{KV/M}$$

One scheme using this arrangement using rotatory motion ~~was~~ has been proposed, with a calculated worst case accuracy of .7 % body mass. The scheme is described in detail in Sec 4. of the Equipment Development Plan and elsewhere.

It consists of a vertical torsion bar to provide restoring force to a horiz. rigid beam with contour couch at the end. The device could be placed in a relatively large oscillation, 2 ft., and the periods measured at two different radii. With knowledge of the period at 2 radii and the spring constant mass may be computed. This device has the disadvantages of size & rather large ^{room} operating ion. Resistance & visceral shift effects might be of importance where

amplitude is large $\Rightarrow$ large ~~vel~~ relatively
large velocities and acceleration.