

Concepts:



Information: Signal must change

τ = time rate of change

amplitude must change above some minimum

$f \propto \frac{1}{\tau}$ C = channel capacity (BW)

$$C = \frac{1}{\tau} \log_2(\eta)$$

η = number of amp. levels

This derivation based on binary bit

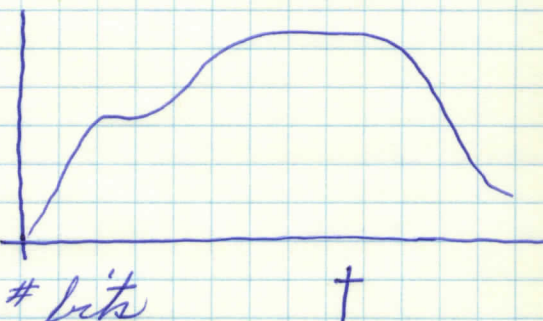
Data Processing:

most info. is in analog.

Analog signal may be digitized

Pulse code modulation is binary.

Levels may be determined 2^n n = # bits



Periodic Signals

Aperiodic

Random - most common in communication sys.

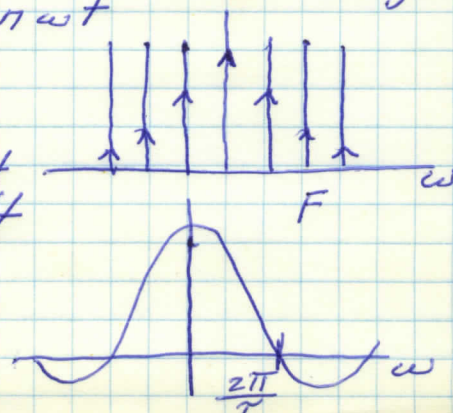
Fourier

$$f(t) = \sum_{n=-\infty}^{\infty} C_n e^{jn\omega t}$$

Periodic signal

Aperiodic

$$F = \int_{-\infty}^{\infty} f(t) e^{-j\omega t} dt$$



Concepts Signal theory contd.

Random Signal.

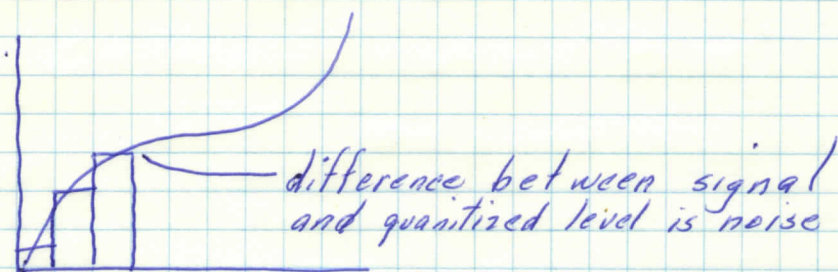
Fourier transform of
auto correlation

$$S(\omega) = \int_{-\infty}^{\infty} R(\tau) e^{-j\omega\tau} d\tau$$

S = power spectral density

Noise: anything other than desired signal

Quantization noise



Thermal noise

$$\underline{n}(t)$$

$\underline{n}$ = function of t ,
normal distribution
average = zero +
flat distribution

Modulation:

$$\text{carrier} = A \cos[\omega_c t + \phi]$$

Modulation may be accomplished
by changing any of these parameters

A = amplitude
 ϕ = phase angle
 $\omega = 2\pi f$

Appello is ϕ mod.

Amplitude modulation: used EVA $\rightarrow$ LEM

$$e(t) = (1 + m f_m(t)) \cos \omega_c t$$

f_m = mod sig -
 m = max. amp. of
mod. signal
= modulation
index

Carrier suppression

$$e_s(t) = m f_m(t) \cos \omega_c t$$

Single sideband, suppressed carrier cannot transmit
pulses -

0830

4 Oct. Communication

P-3 Dawson

NASA SP-69 Space Technology V-5

Phase angle modulation: Apollo + future applications -
telecomm-

$$e(t) = A \cos(\omega_c t + \phi(t))$$

$$= A \cos(\theta(t))$$

$$\theta(t) = \omega_c t + M f_m(t) + \theta_r$$

 θ_r = reference funct.
which is here 0

$$\omega t = \frac{d\theta(t)}{dt}$$

$$= \omega_c + m f_m(t)$$

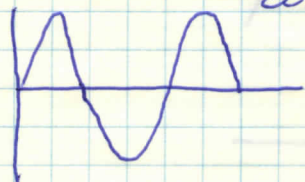
$$\omega(t) = \omega_c + \Delta f \cdot f_m(t)$$

$$\begin{aligned} \theta(t) &= \omega_c t + \Delta f \int f_m(t) dt \\ &\quad + \Delta f \int \cos \omega t dt \\ &= \omega_c t + \frac{\Delta f}{\omega_m} \sin \omega_m t \end{aligned}$$

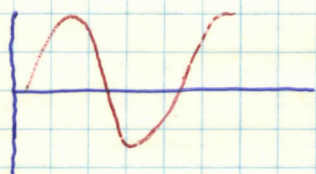
 Δf = peak devia.

$$\frac{\Delta \omega}{\omega_m} = \frac{\Delta f}{f_m} = \beta$$

$$f_m = \cos \omega_m t$$



$$e(t) = A \cos[\omega_c t + \beta \sin \omega_m t]$$



Fourier coefficients are Bessel functs.

$$\cos[\beta \sin \omega_m t] = J(\beta) + 2 \sum_{n=2}^{\infty} J_n(\beta) \cos n \omega_m t$$

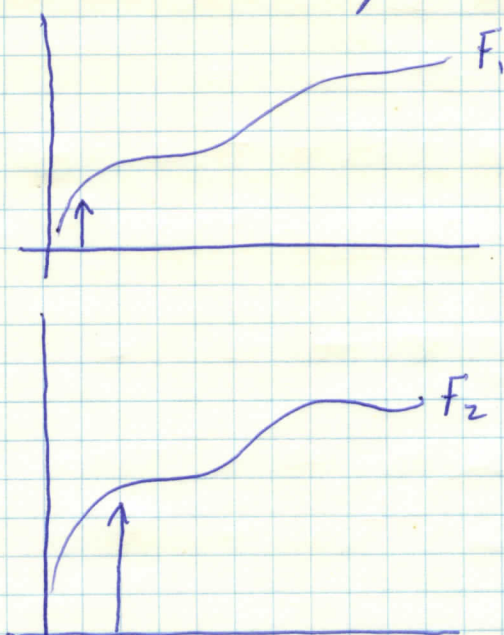
$$\sin[\beta \sin \omega_m t] = 2 \sum_{n=1}^{\infty} J_n(\beta) \sin n \omega_m t$$

At this point degenerated into mass
of math understandable to neither me

In terms of modulation as $\beta \uparrow$ total BW $\uparrow$
See fig. 1+2.

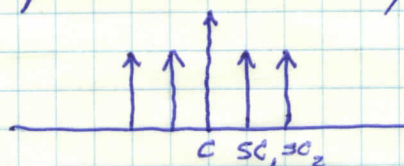
β for phase mod. is constant.

Freq. division multiplex system -

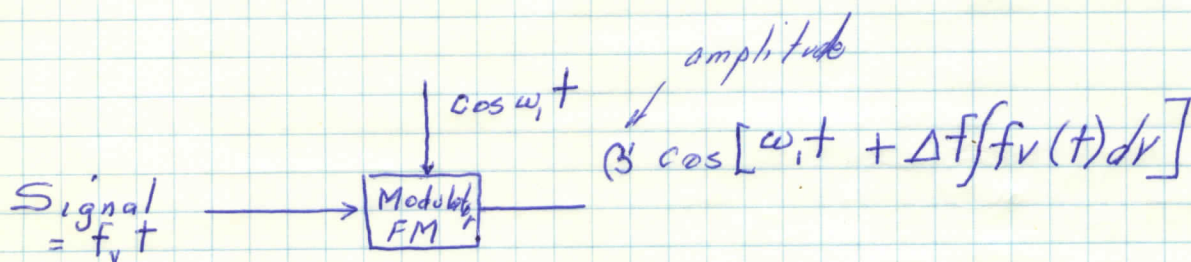


Time sharing multiplex

Time division multiplex -



SC = sub carrier
C = carrier



$$\theta_r = k$$

$$at = \pm 1$$

This signal uses PM

$$e(t) = \cos[\omega_c t + M_1 \sin \omega_1 t + M_2 \sin \omega_2 t + \theta_r a(t)]$$

$$\text{Carrier Power} = P_c = P_R J_0^2(M_{v0}) J_0^2(M_v) \cos^2(\theta_R)$$

$$\text{Tele. Channel Data } P_{v0} = P_R J_0^2(M_{v0}) J_0^2(M_v) \cos^2(\theta_R)$$

$$P_v = P_R J_0^2(M_{v0}) J_0^2(M_v) \cos^2(\theta_R)$$

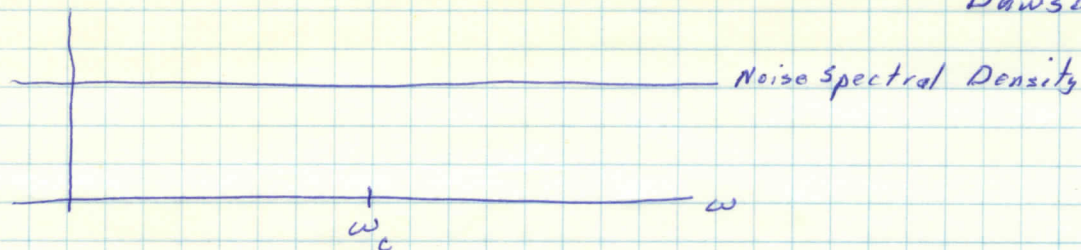
M = Mod. index

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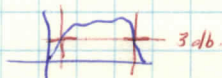
P-5
Dawson

Noise-



Signal Noise Ratio:

$$\frac{E_{sig RMS}}{E_{noise RMS}}$$



$$E = \sqrt{\frac{KTB}{R}}$$

Batson

F.M. Threshold Improvement - Later

Circuit Margin -

$$Db. = 10 \log_{10} \frac{S}{N} = \frac{E\{s^2(t)\}}{E\{n^2(t)\}}$$

Db W is ref. to 1 watt.

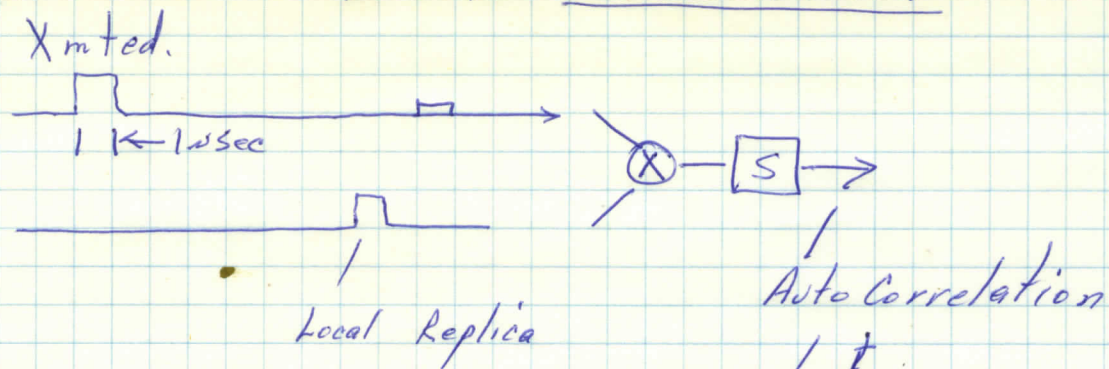
$$\text{Margin} = \frac{(S/N)_{\text{actual}}}{(S/N)_{\text{required}}}$$

Word intelligibility enters this -

Sample circuit margin calculation was explained see Fig 2+3

Ranging: Radar - spin track transponder (used on Apollo)

Pulse radar - envelope detection
correlation " - mixer & main lang-



$$\phi_{11}(\tau) = \int f_1(t) f_1(t+\tau) dt$$

$\phi_{11}(\tau)$

 $|2T|$

Pseudo Random Noise Signals -

Actually periodic signals which possess certain random criteria -

1. balance
2. run
3. correlation